Measurement of Upsilon production in 7 TeV pp collisions at ATLAS

The ATLAS Collaboration

Abstract

Using 1.8 fb\(^{-1}\) of pp collisions at a center-of-mass energy of 7 TeV recorded by the ATLAS detector at the Large Hadron Collider, we present measurements of the production cross sections of \(\Upsilon(1S, 2S, 3S)\) mesons. \(\Upsilon\) mesons are reconstructed using the di-muon decay mode. Total production cross sections for \(p_T < 70\) GeV and in the rapidity interval \(|y^\Upsilon| < 2.25\) are measured to be \(8.01 \pm 0.02 \pm 0.36 \pm 0.31\) nb, \(2.05 \pm 0.01 \pm 0.12 \pm 0.08\) nb, \(0.92 \pm 0.01 \pm 0.07 \pm 0.04\) nb, respectively, with uncertainties separated into statistical, systematic, and luminosity measurement effects. In addition, differential cross section times di-muon branching fractions for \(\Upsilon(1S), \Upsilon(2S),\) and \(\Upsilon(3S)\) as a function of \(\Upsilon\) transverse momentum \(p_T\) and rapidity are presented. These cross sections are obtained assuming unpolarized production. If the production polarization is fully transverse or longitudinal with no azimuthal dependence in the helicity frame the cross section may vary by approximately \(\pm 20\%\). If a non-trivial azimuthal dependence is considered, integrated cross sections may be significantly enhanced by a factor of two or more. We compare our results to several theoretical models of \(\Upsilon\) meson production, finding that none provide an accurate description of our data over the full range of \(\Upsilon\) transverse momenta accessible with this dataset.
Using 1.8 fb$^{-1}$ of $pp$ collisions at a center-of-mass energy of 7 TeV recorded by the ATLAS detector at the Large Hadron Collider, we present measurements of the production cross sections of $\Upsilon(1S, 2S, 3S)$ mesons. $\Upsilon$ mesons are reconstructed using the di-muon decay mode. Total production cross sections for $p_T < 70$ GeV and in the rapidity interval $|y| < 2.25$ are measured to be $8.01 \pm 0.02 \pm 0.36 \pm 0.31$ nb, $2.05 \pm 0.01 \pm 0.12 \pm 0.08$ nb, and $0.92 \pm 0.01 \pm 0.07 \pm 0.04$ nb, respectively, with uncertainties separated into statistical, systematic, and luminosity measurement effects. In addition, differential cross section times di-muon branching fractions for $\Upsilon(1S)$, $\Upsilon(2S)$, and $\Upsilon(3S)$ as a function of $\Upsilon$ transverse momentum $p_T$ and rapidity are presented. These cross sections are obtained assuming unpolarized production. If the production polarization is fully transverse or longitudinal with no azimuthal dependence in the helicity frame the cross section may vary by approximately $\pm 20\%$. If a non-trivial azimuthal dependence is considered, integrated cross sections may be significantly enhanced by a factor of two or more. We compare our results to several theoretical models of $\Upsilon$ meson production, finding that none provide an accurate description of our data over the full range of $\Upsilon$ transverse momenta accessible with this dataset.

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I. INTRODUCTION

Since the discovery of the $J/\psi$ and $\Upsilon$ mesons [1,2] the study of heavy quark-antiquark systems has provided valuable input for our understanding of Quantum Chromodynamics (QCD). However, despite being one of the simplest systems in QCD it has proven difficult historically to describe the production properties of these states adequately. Results on $J/\psi$ and $\Upsilon$ hadroproduction and polarization [3,4] exhibit inconsistencies between measurements and theoretical predictions [5,6].

Measurements at the Large Hadron Collider (LHC) of differential production spectra of various charmonium and bottomonium states together with measurement of their spin-alignments, prompt double-quarkonia production, and production of quarkonia in association with photons, vector bosons or open heavy-flavor final states will allow discrimination between different theoretical approaches based on color-singlet corrections [7–9], color-octet terms [10], the $k_T$-factorization approach [11] and other production models [12,13], and provide additional input toward an improved understanding of quarkonium hadroproduction.

Studies of bottomonium production complement concurrent studies of charmonium systems due to the larger mass of the bottom quark compared to the charm quark, allowing more dependable theoretical calculations than in the charmonium family, which suffer from poor perturbative convergence [14]. Extension of cross-section measurements to higher meson transverse momenta provides valuable input to improvements in the theoretical description since in this regime different processes can dominate and, experimentally, the impact of spin-alignment uncertainties are mitigated.

Taking advantage of the large increase in integrated luminosity delivered by the LHC in 2011, this paper updates a previous measurement [8] and reports the $\Upsilon(1S)$ cross section presented differentially in two intervals of absolute $\Upsilon$ rapidity [9], $|y|$ bins, and fifty intervals of $\Upsilon$ transverse momentum $p_T$, and as a $p_T$-integrated result in forty-five bins of absolute $\Upsilon$ rapidity. In addition, new measurements of the equivalent $\Upsilon(2S)$ and $\Upsilon(3S)$ differential spectra and their production ratios relative to the $\Upsilon(1S)$ are reported.

$\Upsilon$ production can proceed directly, where the $\Upsilon$ meson of interest is produced in the hard interaction, or via the production of an excited state which subsequently decays. This so-called “feed-down” contribution complicates the theoretical description of quarkonium production as calculation of color-singlet $P$-wave and higher orbital angular momentum quarkonium production suffers from the presence of infrared divergences [15]. From the experimental perspective, separation of direct and feed-down contributions is hindered by the small mass splitting between the bottomonium states, which impedes the detection of additional decay products that would indicate indirect production. Contributions from feed-down vary between the $\Upsilon(1S)$, $\Upsilon(2S)$ and $\Upsilon(3S)$ states due to the changing presence of various kinematically-allowed decays and influence the inclusive production rate. Study of the $\Upsilon$ production ratios as a function of kinematic variables as presented here thus provides an indirect but precise measure of these feed-down contributions.

This new analysis extends the $p_T$ range of our previous cross-section result $\S$ to 70 GeV, at which new contributions to $\Upsilon$ production [12,16] such as from associated $\Upsilon + b\bar{b}$ production may play a more important role and the impact of the dependence of the production cross section on the spin-alignment of the $\Upsilon$ is relatively small. Both the fiducial cross section, measured in the kinematic region with muon transverse momentum $p_T^\mu > 4$ GeV and muon pseudorapidity $|\eta^\mu| < 2.3$, and the corrected cross section, which is defined in this paper as the cross section in the $p_T-\eta$ phase space of the $\Upsilon$ corrected for the acceptance of the decay products to the full $\Upsilon$ production phase space, are reported. In the former case, the
results have no dependence on assumptions about $\Upsilon$ spin alignment, while the latter measurements are more easily compared to model predictions and to the results of other experiments.

II. THE ATLAS DETECTOR

The ATLAS detector is composed of an inner tracking system, calorimeters, and a muon spectrometer. The inner detector directly surrounds the interaction point and consists of a silicon pixel detector, a silicon microstrip detector, and a transition radiation tracker, all immersed in a 2T axial magnetic field. It covers the pseudorapidity range $|\eta| < 2.5$ and is enclosed by a calorimeter system containing electromagnetic and hadronic sections. Surrounding the calorimeters is the large muon spectrometer built with three air-core toroids. This spectrometer is equipped with precision detectors (monitored drift tubes and cathode strip chambers) that provide precise measurements in the bending plane within the pseudorapidity range $|\eta| < 2.7$. In addition, resistive plate and thin gap chambers with fast response times are used primarily to reconstruct muon triggers in the ranges $|\eta| < 1.05$ and $1.05 < |\eta| < 2.4$ respectively, but are also used to provide position measurements in the non-bending plane and to improve pattern recognition and track reconstruction. Momentum measurements in the muon spectrometer are based on track segments formed in at least two of the three precision chamber planes.

The ATLAS detector employs a three-level trigger system, which reduces the 20 MHz proton bunch collision rate to the several hundred Hz transfer rate to mass storage. The Level-1 muon trigger searches for hit coincidences between different muon trigger detector layers inside pre-programmed geometrical windows that bound the path of triggered muons of given transverse momentum and provide a rough estimate of its position within the pseudorapidity range $|\eta| < 2.4$. At Level-1, muon candidates are reported in “regions of interest” (RoIs). Only a single muon can be associated with a given RoI of spatial extent $\Delta \phi \times \Delta \eta \approx 0.1 \times 0.1$. This limitation has a small effect on the trigger efficiency for $\Upsilon$ mesons, corrected for in the analysis using a data-driven method based on analysis of $J/\psi \rightarrow \mu^+\mu^-$ and $\Upsilon \rightarrow \mu^+\mu^-$ decays. The Level-1 trigger is followed in sequence by two subsequent higher-level, software-based trigger selection stages. Muon candidates reconstructed at these higher levels incorporate, with increasing precision, information from both the muon spectrometer and the inner detector and reach position and momentum resolution close to that provided by the offline muon reconstruction.

III. DATASET AND EVENT SELECTION

Data for this study were collected during the 2011 LHC proton-proton running period between March and August using a trigger that requires the presence of two muon candidates with opposite charges that are subject to a fit constraining them to a common vertex while taking into account track parameter uncertainties. A very loose selection on vertex $\chi^2$ which is fully efficient for signal candidates, was imposed to ensure proper fit convergence, as well as the requirement of opposite charge and that $p_T^\mu > 4$ GeV and $|\eta^\mu| < 2.3$. This trigger was largely unprescaled and collected data at a rate of approximately 20 Hz in this period of data-taking.

Events are required to contain at least one primary vertex candidate that has at least five tracks with $p_T > 0.4$ GeV, and at least two muons identified by associating candidates found in the muon spectrometer with tracks reconstructed in the inner detector. Multiple scattering in the calorimeters and toroids of the ATLAS detector degrades the muon spectrometer resolution for low energy particles. As the majority of muons selected for this analysis have low momentum, we assign values for parameters such as $p_T$ and $\eta$ to the muons based on track fits using inner detector information only. To ensure accurate inner detector measurements, each muon track must contain at least six silicon microstrip detector hits and at least one pixel detector hit. Muon candidates passing these criteria are required to have $p_T^\mu > 4$ GeV and $|\eta^\mu| < 2.3$ and a successful fit to a common vertex.

Good spatial matching ($\Delta R \equiv \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2} < 0.01$) between the muon candidate in both the offline reconstruction and the trigger used to select the event is required to facilitate data-driven estimates of the di-muon trigger efficiency. Furthermore, both muons forming a $\Upsilon$ candidate must be associated to their trigger-level candidates in this manner. In this way, the efficiency of the trigger requirements on the di-muon candidate are incorporated into the trigger efficiency correction. All di-muon candidates passing these criteria are retained for analysis.

The distribution of the invariant mass of the $\mu^+\mu^-$ system is shown in Fig. 1 for the selected di-muon candidates. As is apparent from the plot, the mass resolution (120 MeV) for di-muon candidates detected in the central region of the detector ($|y^{\mu\mu}| < 1.2$) is significantly better than the resolution (214 MeV) for those candidates falling into the forward region ($1.2 \leq |y^{\mu\mu}| < 2.25$). A total of $3.9 \times 10^6$ and $2.3 \times 10^6$ candidates with $8 < m_{\mu\mu} < 11.5$ GeV are reconstructed in the central and forward regions respectively.
Determination of the cross sections proceeds through several steps. Firstly, a weight, \( w \), is determined for each \( \Upsilon \) candidate equal to the inverse of the total signal plus background shape (solid curve). The background shape is modelled here by a fourth-order polynomial and the signal peaks each modelled by a single Gaussian. Also quoted are the fitted mass resolutions of each of the three signal peaks, determined from the fit with a common resolution parameter scaling with invariant mass.

\[ \frac{d^2\sigma}{dp_T dy} \times \text{Br}(\Upsilon \rightarrow \mu^+\mu^-) = \frac{N_T}{\int L dt \times \Delta p_T \times \Delta|y|} \]  

where \( \text{Br}(\Upsilon \rightarrow \mu^+\mu^-) \) represents the appropriate branching fraction of the \( \Upsilon(nS) \) to di-muons, \( \int L dt \) is the integrated luminosity, \( \Delta p_T \) and \( \Delta|y| \) are the bin sizes in \( \Upsilon \) transverse momentum and rapidity, respectively, and \( N_T \) is the corrected number of observed \( \Upsilon(1S), \Upsilon(2S), \) or \( \Upsilon(3S) \) mesons in a bin. Corrections are applied to account for selection efficiencies, bin migration effects due to finite detector resolution, and, in the case of corrected cross-section measurements, acceptance.

Determination of the cross sections proceeds through several steps. Firstly, a weight is determined for each selected di-muon candidate equal to the inverse of the total efficiency for the candidate. Secondly, a fit is performed to the distribution of weighted events binned in di-muon invariant mass, \( m_{\mu\mu} \), to determine the number of \( \Upsilon(nS) \) mesons (with \( n = 1,2,3 \)) produced in each \( (p_T^{\mu\mu}, y^{\mu\mu}) \) bin. Thirdly, these values are corrected for \( (p_T^{\mu\mu}, y^{\mu\mu}) \) bin migrations. Finally, the differential cross section multiplied by the \( \Upsilon \rightarrow \mu^+\mu^- \) branching fraction is calculated for each state using the integrated luminosity and the \( p_T \) and \( y \) bin widths as in Eq. (1).

The weight, \( w \), for each \( \Upsilon \) candidate includes the fraction of produced \( \Upsilon \rightarrow \mu^+\mu^- \) decays with both muons falling into the kinematic region \( p_T^{\mu} > 4 \text{ GeV} \) and \( |y^{\mu}| < 2.3 \) (the acceptance, \( A \), is used only in calculating corrected cross sections), the probability that a candidate falling within the acceptance passes the offline reconstruction requirements (the reconstruction efficiency, \( \varepsilon_{\text{reco}} \)), and the probability that a reconstructed event passes the trigger selection (the trigger efficiency, \( \varepsilon_{\text{trig}} \)). The weights assigned to a given candidate when calculating the fiducial \( (w_{\text{fid}}) \) and corrected \( (w_{\text{tot}}) \) cross sections are then given by:

\[ w_{\text{fid}} = \left( \varepsilon_{\text{reco}} \cdot \varepsilon_{\text{trig}} \right)^{-1}, \]

\[ w_{\text{tot}} = \left( A \cdot \varepsilon_{\text{reco}} \cdot \varepsilon_{\text{trig}} \right)^{-1}. \]  

### A. Acceptance

The kinematic acceptance \( A(p_T, y) \) is the probability that the muons from an \( \Upsilon \) with transverse momentum \( p_T \) and rapidity \( y \) fall into the fiducial volume of the detector defined by the \( p_T^{\mu} > 4 \text{ GeV} \) and \( |y^{\mu}| < 2.3 \) selection applied to each muon in the di-muon pair. In order to calculate the acceptance as a function of the rapidity and transverse momentum of each of the \( \Upsilon \) states, taking into account possible angular dependences in their decays, we use an analytic formula describing the decay of \( \Upsilon \) states.

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**FIG. 1:** The di-muon invariant mass spectrum for events used in this analysis. Separate spectra are shown for those events with the di-muon candidate (left) in the central region of the detector \( (|y| < 1.2) \) and (right) in the forward region \( (1.2 < |y| < 2.25) \). Overlaid are individual shapes of the fitted \( \Upsilon(nS) \) signals (shaded regions), background-only fit (dashed curve) and the total signal plus background shape (solid curve). The background shape is modelled here by a fourth-order polynomial and the signal peaks each modelled by a single Gaussian. Also quoted are the fitted mass resolutions of each of the three signal peaks, determined from the fit with a common resolution parameter scaling with invariant mass.
in their decay frame \[24\],

\[
\frac{d^2 N}{d \cos \theta^* d \phi^*} \propto 1 + \lambda_\theta \cos^2 \theta^* + \lambda_\phi \sin^2 \theta^* \cos 2\phi^* \\
+ \lambda_{\theta\phi} \sin 2\theta^* \cos \phi^*. \tag{3}
\]

The helicity frame is used, where \( \theta^* \) is the polar angle between the \( \mu^+ \) momentum in the \( \Upsilon \) decay frame and the direction of the \( \Upsilon \) momentum in the laboratory frame. The corresponding azimuthal angle \( \phi^* \) is the angle between the quarkonium production plane (defined in the quarkonium decay frame by the two momenta of the incoming protons in that frame) and the quarkonium decay plane in the lab frame.

The \( \lambda_i \) coefficients parameterize the spin-alignment state of the \( \Upsilon \). In some parts of the phase space the acceptance may depend on these parameters quite strongly. We have identified five extreme cases that lead to the largest possible variations of acceptance within the phase space of this measurement and define an envelope in which the results may vary under any physically-allowed spin-alignment assumption: isotropic distribution independent of \( \theta^* \) and \( \phi^* \) (\( \lambda_\theta = \lambda_\phi = \lambda_{\theta\phi} = 0 \), labeled FLAT); longitudinal alignment (\( \lambda_\theta = -1, \lambda_\phi = \lambda_{\theta\phi} = 0 \), labeled LONG); and three types of transverse alignment (\( \lambda_\theta = +1, \lambda_\phi = \lambda_{\theta\phi} = 0 \), labeled \( T+0 \); \( \lambda_\theta = +1, \lambda_\phi = +1, \lambda_{\theta\phi} = 0 \), labeled \( T++ \); \( \lambda_\theta = +1, \lambda_\phi = -1, \lambda_{\theta\phi} = 0 \), labeled \( T+- \)). The central values of our measurements are derived under the isotropic production assumption. The spread in corrected cross-section results derived under all five assumptions is used to quantify the full envelope of possible variations of the result due to spin-alignment. Some constraints on physically-allowed \( \lambda_i \) combinations exist \[24, 25\]. In particular, \( \lambda_{\theta\phi} \) must be zero for \( \lambda_\theta = \pm 1 \) and any \( \lambda_\phi \), and \( |\lambda_{\theta\phi}| \leq 0.5 \) for \( \lambda_\theta = \lambda_\phi = 0 \). Acceptance corrections with non-zero \( \lambda_{\theta\phi} \) were found to lead to corrections with smaller or equal variations from the isotropic scenario than any parameter-space scenarios on the \( \lambda_\theta-\lambda_\phi \) plane. Acceptance weights for each polarization scenario, including those with non-zero \( \lambda_{\theta\phi} \), can be found in HEPDATA \[26\].

Figure 2 presents the two-dimensional acceptance map for \( \Upsilon(1S) \), as a function of the \( \Upsilon \) transverse momentum and absolute rapidity in the unpolarized (FLAT) acceptance scenario as well as the maximum relative variation (ratio of largest to smallest acceptance correction) of the acceptance maps across all spin-alignment scenarios.

Acceptance is significantly decreased at very high rapidities due to the muon pseudorapidity requirement of \(|\eta^\mu| < 2.3\). When \( \Upsilon \) are produced at rest, both muons are likely to be reconstructed in the muon spectrometer on opposite sides of the detector. When the \( \Upsilon \) has a sufficient boost, the two muons are more likely to be found in the same side of the detector and the probability that at least one muon is below the required \( p_T^\mu \) threshold increases, leading to a drop in acceptance. At higher \( p_T \) the \( \Upsilon \) imparts greater momentum to the two muons, the likelihood of a muon being below threshold decreases and the acceptance asymptotically approaches 100%. As \( \Upsilon \) transverse momentum increases the variation of the acceptance corrections between spin-alignment scenarios decreases, becoming \( \lesssim 10\% \) at the largest \( p_T \) ranges studied. Similar behaviours are observed in the acceptance maps for the \( \Upsilon(2S) \) and \( \Upsilon(3S) \).

This spin-alignment systematic uncertainty only applies to the corrected cross-section measurements. For fiducial cross sections, measured in the kinematic region
from (rather than toward for the opposing charge) the middle/outer spectrometer planes, they will not be identified as muons.

The efficiency of the di-muon trigger to select events that have passed the offline selection criteria, $\varepsilon_{\text{trig}}$, is also calculated from data. This can be factorized into three terms:

$$
\varepsilon_{\text{trig}} = \varepsilon_{\text{RoI}}(p_T^{\mu_1}, q_1 \cdot \eta_1^\mu) \times \varepsilon_{\text{RoI}}(p_T^{\mu_2}, q_2 \cdot \eta_2^\mu) \times c_{\text{mu}}(\Delta R, |y^{\mu\mu}|)
$$

where $\varepsilon_{\text{RoI}}$ is the efficiency of the trigger system to find an RoI for a single muon with transverse momentum, $p_T^{\mu}$, and charge-signed pseudorapidity, $q \cdot |\eta^{\mu}|$, and $c_{\text{mu}}$ is a correction for effects related to the di-muon elements of the trigger. This correction accounts for the di-muon vertex and opposite charge requirements, and for loss of efficiency in the di-muon trigger if the two muons are close enough together to register only as a single RoI.

The di-muon correction, $c_{\text{mu}}$, itself consists of two components

$$
c_{\text{mu}}(\Delta R, y^{\mu\mu}) = c_a(y^{\mu\mu}) \times c_{\Delta R}(\Delta R, y^{\mu\mu})
$$

each evaluated in three separate regions of di-muon rapidity: barrel ($|y^{\mu\mu}| \leq 1.0$), barrel-endcap transition ($1.0 < |y^{\mu\mu}| < 1.2$), and endcap ($1.2 \leq |y^{\mu\mu}| < 2.25$), to account for the different behaviors of these corrections in these regions. The correction $c_a$ is due to the effect of vertex and opposite charge requirements on the trigger and is determined from the efficiency at large di-muon angular separations. No difference was observed from deriving the result as a function of $\Delta y$ and $\Delta \phi$ separately rather than versus $\Delta R$. The asymptotic values are found using the ratio of candidate $J/\psi \rightarrow \mu^+ \mu^-$ decays selected by the standard di-muon trigger to those selected by a similar di-muon trigger that makes no charge or vertex requirements. These values are found to be $99.1 \pm 0.4\%$, $97.5 \pm 0.9\%$, $95.2 \pm 0.4\%$ in the barrel, transition, and endcap regions, respectively.

We extract this dependence on $\Delta R$ in the same three regions of di-muon rapidity as used for $c_a$ from a sample of offline selected $J/\psi \rightarrow \mu^+ \mu^-$ candidates with $p_T^{\mu} > 8 \text{ GeV}$ using a single-muon trigger with a threshold of 18 GeV. The 8 GeV requirement on the lower $p_T$ muon is made to ensure that the efficiency for the trigger system to identify RoIs compatible with muons of $p_T > 4 \text{ GeV}$ reached its plateau value. The $\Delta R$ dependence of $c_{\Delta R}$ is then extracted from the fraction of fitted di-muon candidates in a $\Delta R$ interval within this control sample selected using auxiliary triggers that additionally pass the di-muon trigger used in this analysis.

The final component of the di-muon trigger efficiency, $\varepsilon_{\text{RoI}}$, represents the single-muon trigger efficiency with a threshold of $p_T^{\mu} > 4 \text{ GeV}$. This is measured using well-reconstructed $J/\psi \rightarrow \mu^+ \mu^-$ candidates in data that pass a single-muon trigger (with a threshold of 18 GeV). The ratio of the yield of $J/\psi$ candidates (determined by fitting the invariant mass distributions) that pass both this
single-muon trigger and the 4 GeV $p_T^\mu$ threshold di-muon trigger used in this analysis, to the yield of $J/\psi$ candidates that pass the single-muon trigger is identified as the single-muon trigger efficiency $\varepsilon_{\text{Red}}$ in the $p_T^\mu$ and $q |y^\mu|$ interval considered. In each case, the reconstructed muon(s) are matched to the muon(s) that triggered the event for each of the single or di-muon triggers. The number of candidates passing the di-muon trigger is then further corrected by $\varepsilon_{\mu\mu}$ for di-muon correlation effects [22].

The individual and overall efficiencies and weight corrections, calculated using the methods described above, are shown as functions of $p_T^{\mu\mu}$ and $|y^{\mu\mu}|$ in Fig. 8 for the $\Upsilon(1S)$.

C. Extracting the number of $\Upsilon$ mesons

The number of produced $\Upsilon(nS)$ mesons used in our cross-section determination is found by fitting signal and background functions to the $m_{\mu\mu}$ spectrum of weighted $\Upsilon$ candidates. The use of per-candidate weights rather than average weights allows us to correct for acceptance and efficiency without introduction of biases associated with the use of average values for these quantities. We determine the $\Upsilon$ differential cross sections separately for each spin-alignment scenario. We perform least squares fits to $m_{\mu\mu}$ histograms filled using the weights, $w$, for each candidate in bins of di-muon transverse momentum, $p_T^{\mu\mu}$, and rapidity, $y^{\mu\mu}$. The form of the $\chi^2$ for each ($p_T^{\mu\mu}$, $|y^{\mu\mu}|$) bin is:

$$\chi^2 = \sum_{i=m_{\mu\mu}^{\text{bin}}} \left( \frac{n_i^{\text{data}} - n_i^{\text{pred}}}{\sigma_i} \right)^2$$

where $N_i$ represents the number of $\Upsilon(nS)$ candidates in bin $i$.

Predictions for each bin are constructed using four sources of di-muon candidates:

$$n^{\text{pred}}(m_{\mu\mu}) = N_{1S}F_{1S}(m_{\mu\mu}; f_{1S}) + N_{2S}F_{2S}(m_{\mu\mu}; f_{2S}) + N_{3S}F_{3S}(m_{\mu\mu}; f_{3S}) + F_{\text{bgd}}(m_{\mu\mu}; f_{\text{bgd}})$$

where the $f_X$ here represent fit function parameters and the $F_X$ are normalized probability density functions. In order to avoid bias due to the choice of fit model, several parameterizations of signal and background, which describe the data well, are used.

Each of the three $\Upsilon$ resonances are parameterized by single Gaussian, double Gaussian, or Crystal Ball functions, chosen to provide a reasonable description of the experimental mass resolution and energy loss effects that dominate the observed signal line-shapes. The background parameterizations vary with di-muon $p_T$. At low

![FIG. 3: Efficiency and acceptance corrections contributing to the overall fiducial and corrected efficiencies (and the inverse of the efficiency, the weight) as a function of the $\Upsilon(1S)$ $p_T^{\mu\mu}$ in the central (top) and forward (middle) regions of the detector and as a function of $|y^{\mu\mu}|$ (bottom).](image-url)
FIG. 4: Fits to the efficiency-corrected $m_{\mu\mu}$ spectra for candidates in the low (0.5–1.0 GeV; top), mid (20–21 GeV; middle), and high (40–45 GeV; bottom) $p_T$ intervals, for central (left) and forward (right) di-muon rapidities. Fit results are shown for the simplest fit model considered: a single Gaussian signal plus either a second-order polynomial multiplied by an error function (low $p_T$), second-order polynomial (mid $p_T$), or first-order polynomial (high $p_T$) background parameterization.
$p_T^{\mu\mu}$, and for all rapidity bins, an error function multiplied by either a second-order polynomial, or a second-order polynomial plus an exponential, is used to model $m_{\mu\mu}$ turn-on effects accurately. At mid $p_T^{\mu\mu}$ a second-order polynomial, or second-order polynomial plus an exponential is adequate to describe the shape of the background under the $T$ peaks. At high $p_T^{\mu\mu}$ a first-order polynomial or a first-order polynomial plus an exponential is sufficient to describe the background contribution. Average fitted values for the numbers of $T(nS)$ mesons ($N_{1S}$, $N_{2S}$, $N_{3S}$) taken over all combinations of signal and background models are used in the extraction of cross sections, while the maximum deviation of any fit result from the average is used as an estimate of the fit model systematic uncertainty.

In the fits $N_{1S}$, $N_{2S}$, $N_{3S}$, the peak mass of the $T(1S)$ meson ($M_{1S}$), parameters describing the shape of the $T \rightarrow \mu^+\mu^-$ mass distribution, and the background parameters are allowed to vary freely while $M_{2S}$, $M_{3S}$ are fixed relative to $M_{1S}$ using measured mass splittings [22]; and the line-shape width parameters $\sigma_{2S}$, $\sigma_{3S}$ are related linearly in $m_{\mu\mu}$ to $\sigma_{1S}$. The distribution of the $\chi^2$-probabilities from the fits are uniformly distributed indicating that our signal and background parameterizations provide good descriptions of the data. Figure 4 shows the invariant mass distribution of the fitted signal region for representative low, mid, and high $T$ $p_T$ intervals, in both the central and forward rapidity regions.

In order to account for bin migrations due to finite detector resolution, corrections in $p_T^{\mu\mu}$ are derived by first fitting a smooth analytic function to the background-subtracted $p_T^{\mu\mu}$ spectra of $T$ events in data. This fitted distribution is deconvolved with a Gaussian distribution using a Gauss-Hermite quadrature integration technique, with a $p_T$ resolution derived from the fitted invariant mass and muon angular resolutions in data. From the distributions with and without convolution, migration corrections bin-by-bin are derived. These corrections are found to be within 0.5% of unity for central rapidities and within 1% of unity for forward rapidities. The number of efficiency-corrected $T \rightarrow \mu^+\mu^-$ decays extracted from the fits in each $(p_T^{\mu\mu}, y^{\mu\mu})$ bin are corrected for the difference between true and reconstructed values of the di-muon $p_T$ and rapidity. Using a similar technique, bin-migration corrections as functions of $y^{\mu\mu}$ are found to be negligible.

V. SYSTEMATIC UNCERTAINTIES

We consider the following sources of systematic uncertainty on the $T(nS)$ differential cross sections: luminosity determination, reconstruction and trigger efficiencies, migration between $p_T^{\mu\mu}$ and $y^{\mu\mu}$ bins due to resolution, acceptance corrections, and the background and signal fit models used. The range of these uncertainties for the three $T$ states is summarized in Table 3 and their breakdown in each source is given for the corrected cross-section analysis in Figs. 5–7.

The relative luminosity uncertainty of 3.9% is described in more detail in Ref. [23]. Other sources of systematic uncertainty are discussed below. As the statistical components of the uncertainties associated with the determination of $\varepsilon_{\text{reco}}$ and $\varepsilon_{\text{trig}}$ are dominant, the uncertainties on the cross sections are derived from the statistics of the control samples used to extract them using a series of pseudo-experiments, randomly varying the weights used for each $T$ candidate in data, according to the uncertainties on the efficiency maps. Systematic uncertainties associated with the fit model used to extract the number of $T(nS)$ decays from our di-muon data sample, are quantified by taking the largest deviation of the fitted values of $N_{nS}$ found in the six possible model combinations from the average value. Systematic effects, due to differences in the underlying kinematic distributions of the control sample and the data distributions, are found to be negligible due to the fine differential binning of the efficiency and acceptance corrections.

Uncertainties associated with the acceptance correction include statistical uncertainties on the determination of the correction in fine $p_T$ and rapidity bins. This constitutes approximately a 0.5% uncertainty across the measured spectrum. A shift in the interaction point along the beamline axis, $z$, influences the acceptance particularly at large rapidity. To estimate the impact of this effect, the acceptances were recalculated with shifts in $z$ by ±62 mm, corresponding to one Gaussian standard deviation of the vertex $z$ position distribution in the analyzed data, and the variation in the measured cross sections was calculated as a function of $T$ $p_T$ and rapidity. These variations result in uncertainties on the acceptance corrections of 0.4–0.7% as a function of $p_T$, and 0.6–1.5% as a function of rapidity, growing toward larger rapidities and lower transverse momenta. Our estimate of the correction to the number of $T \rightarrow \mu^+\mu^-$ decays fitted in each $(p_T^{\mu\mu}, y^{\mu\mu})$ bin for differences between reconstructed and true values of $p_T^{\mu\mu}$ due to bin migration depends on a knowledge of the di-muon $p_T$ resolution. Allowing this resolution to vary within its uncertainty results in a negligible change in the $T(nS)$ cross sections.

As mentioned earlier, $T$ spin-alignment effects have an impact on the determination of cross sections extrapolated to full phase space. As in the ATLAS measurement of $J/\psi$ production [7], we quote an uncertainty due to $T$ spin-alignment by comparing results obtained using the unpolarized assumption ($\lambda_0 = \lambda_\phi = \lambda_{\phi\phi} = 0$) to those derived under the other four extreme parameter combinations. The size of the possible variation in each bin is taken to be the largest positive and negative deviation from the unpolarized baseline result. We provide the cross-section results for each of the spin-alignment scenarios along with tabulated values [26] of the weight corrections so that the corrected data can be determined in terms of any spin-alignment scenario.
TABLE I: Summary of statistical and systematic uncertainties on the cross-section measurements. The systematic uncertainty due to the acceptance determination applies only to the corrected cross-section measurements and does not include possible variation of the result due to spin-alignment. Values quoted refer to the range of uncertainties over $p_T^{\mu\mu}$ in each of the $y^{\mu\mu}$ regions considered.

<table>
<thead>
<tr>
<th>Source</th>
<th>Relative Uncertainty $[\Upsilon(1S) / \Upsilon(2S) / \Upsilon(3S)]$ [%]</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$</td>
</tr>
<tr>
<td>Statistical Uncertainty</td>
<td>1.5–10 / 2–10 / 3–10</td>
</tr>
<tr>
<td>Fit Model</td>
<td>0.3–2 / 0.3–10 / 0.3–15</td>
</tr>
<tr>
<td>Luminosity</td>
<td>3.9</td>
</tr>
<tr>
<td>Trigger Efficiency</td>
<td>2.0–3.0 / 1.0–2.0 / 1.0–2.0</td>
</tr>
<tr>
<td>Muon Reconstruction Efficiency</td>
<td>0.7–2.0 / 0.4–1.2 / 0.4–1.2</td>
</tr>
<tr>
<td>Acceptance corrections</td>
<td>0.7–1.5</td>
</tr>
<tr>
<td>Track Reconstruction Efficiency</td>
<td>1.0</td>
</tr>
</tbody>
</table>

FIG. 5: Sources of statistical and systematic uncertainty on the corrected $\Upsilon(nS)$ production cross-section measurements in the central rapidity region. A common luminosity uncertainty of ±3.9% is not included.
VI. RESULTS AND DISCUSSION

We measure the differential cross section multiplied by the di-muon branching fractions of Υ(1S), Υ(2S), and Υ(3S) mesons as a function of Υ transverse momentum and rapidity, both in a fiducial region defined by $p_T^\mu > 4 \text{ GeV}$, $|\eta^\mu| < 2.3$ (free from spin-alignment uncertainties), and corrected back to the full muon decay phase space with $|y^\Upsilon| < 2.25$. We additionally present measurements of the production cross sections of the Υ(2S) and Υ(3S) relative to the Υ(1S) as a function of Υ(1S) transverse momentum and rapidity. Tabulated results of all measurements presented in this paper are available in HEpdata [26].

A. Fiducial cross sections

Corrected cross section

$1.2 \leq |y^{\mu\mu}| < 2.25$

- Total uncertainty
- Statistical
- Total systematics
- Muon reconstruction
- Trigger
- Inner Detector tracking
- Acceptance
- Fit model

FIG. 6: Sources of statistical and systematic uncertainty on the corrected Υ(nS) production cross-section measurements in the forward rapidity region. A common luminosity uncertainty of ±3.9% is not included.
FIG. 7: Sources of statistical and systematic uncertainty on the corrected \( \Upsilon(nS) \) production cross-section measurements as a function of \( \Upsilon \) rapidity. A common luminosity uncertainty of \( \pm 3.9\% \) is not included.

to a significantly higher \( p_T \) and with increased precision.

TABLE II: Integrated fiducial cross-section measurements for \( \Upsilon(nS) \). Uncertainties quoted represent statistical, systematic, and luminosity terms respectively:

<table>
<thead>
<tr>
<th>State</th>
<th>( \sigma_{fid}(pp \rightarrow \Upsilon) \times \text{Br}(\Upsilon \rightarrow \mu^+\mu^-) )</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( p_T &gt; 70 \text{ GeV},</td>
</tr>
<tr>
<td>( \Upsilon(1S) )</td>
<td>( 1.890 \pm 0.007 \pm 0.095 \pm 0.074 \text{ nb} )</td>
</tr>
<tr>
<td>( \Upsilon(2S) )</td>
<td>( 0.601 \pm 0.003 \pm 0.040 \pm 0.023 \text{ nb} )</td>
</tr>
<tr>
<td>( \Upsilon(3S) )</td>
<td>( 0.304 \pm 0.003 \pm 0.021 \pm 0.012 \text{ nb} )</td>
</tr>
</tbody>
</table>

Presenting the results in a restricted kinematic phase space removes any uncertainty due to the spin-alignment of quarkonia. This allows unambiguous comparison of differential spectra with any theoretical approaches which can provide predictions with kinematic restrictions applied to the decay products of the \( \Upsilon \).

NLO color-singlet [14] predictions [30] have previously been compared to differential \( \Upsilon(1S) \) fiducial production cross sections [8] and were found to underestimate the measured production rates by approximately an order of magnitude and to not reflect the \( p_T \) dependence of the data. This is not surprising as it has been known [16] for some time that higher-order corrections are both large and necessary in order to adequately describe quarkonium production at high \( p_T \) with color-singlet terms. At this time, no color-singlet calculations beyond NLO
FIG. 8: Differential cross sections multiplied by the di-muon branching fraction, \(d^2\sigma/dp_T dy \times \text{Br}(\Upsilon \rightarrow \mu^+\mu^-)(p_T\text{-integrated})\), for central (top) and forward (bottom) rapidities, for \(\Upsilon(1S), \Upsilon(2S), \Upsilon(3S)\) production within the fiducial acceptance. Points with error bars indicate results of the measurements with statistical uncertainties while shaded areas correspond to total uncertainties on the measurement, including systematic effects.

FIG. 9: Differential cross sections multiplied by the di-muon branching fraction, \(d\sigma/dy \times \text{Br}(\Upsilon \rightarrow \mu^+\mu^-)(p_T\text{-integrated})\) for \(\Upsilon(1S), \Upsilon(2S), \Upsilon(3S)\) production within the fiducial acceptance. Points with error bars indicate results of the measurements with statistical uncertainties while shaded areas correspond to total uncertainties on the measurement, including systematic effects.

B. Corrected cross sections

We also calculate differential cross sections multiplied by the \(\Upsilon \rightarrow \mu^+\mu^-\) branching fractions extrapolated to the full muon phase space within \(|y^\Upsilon| < 2.25\). For these corrected cross sections, the results of fits to di-muon candidates in data are corrected, candidate by candidate, for efficiencies using the total weights, \(w_{\text{tot}}\), defined in Eq. (2). Results are shown for the isotropic spin-alignment scenario in Figs. 10 and 11 as a function of \(p_T\) and \(y\) for all three states and, integrated over all \(p_T\) and both rapidity bins, in Table III.

Our results are consistent with measurements by CMS [6] and, in the small region of rapidity overlap from \(2.0 < |y| < 2.25\), with LHCb [11]. These results allow us to test phenomenological models of \(\Upsilon\) production not just at low \(p_T\) (for complementarity with results from the Tevatron experiments) but in a newly-probed region of significantly boosted \(\Upsilon\), where higher-order contributions become particularly important.

Figures 12–17 show the differential cross sections as a function of \(p_T\) and rapidity for each of the \(\Upsilon\) states in comparison with theoretical predictions. The effects of varying spin-alignment assumptions from the nominal assumption of isotropic muon angular distributions independent of \(\theta^\mu\) and \(\phi^\mu\) are indicated by a shaded band.

Clearly, spin-alignment has a large effect on the \(\Upsilon\) production cross sections, especially at low \(p_T^\Upsilon\), and in partic-
ular if there is a non-trivial azimuthal component to the spin-alignment. New results [4, 12] of Υ spin-alignment from CDF and CMS suggest that the spin-alignment is consistent with unpolarized production. Our central assumption of isotropic Υ decays is consistent with these results. Nevertheless, as these spin-alignment measurements are made at different center-of-mass energies or in a restricted phase space in both $p_T$ and rapidity with respect to measurements presented here, we provide the

\begin{table}[h]
\centering
\begin{tabular}{|c|c|}
\hline
State & $\sigma(pp \to \Upsilon) \times Br(\Upsilon \to \mu^+ \mu^-)$ \\
\hline
$\Upsilon$(1S) & $8.01 \pm 0.02 \pm 0.36 \pm 0.31 \text{ nb}$ \\
$\Upsilon$(2S) & $2.05 \pm 0.01 \pm 0.12 \pm 0.08 \text{ nb}$ \\
$\Upsilon$(3S) & $0.92 \pm 0.01 \pm 0.07 \pm 0.04 \text{ nb}$ \\
\hline
\end{tabular}
\end{table}

results under a variety of polarization scenarios so that the impact of spin-alignment on the corrected cross sections can be quantified across the full range of study.

The contributions of the five polarization scenarios can be seen in the lower panes of each plot where the ratio of the differential cross section under these spin-alignment assumptions to the unpolarized scenario is shown. Across the whole $p_T$ range studied the envelope is bounded from above by the $T^{++} (\lambda_\theta = +1, \lambda_\phi = +1, \lambda_{\phi\theta} = 0)$ scenario with a maximal $\phi^*$ variation. From below, the cross-section envelope is bounded by fully longitudinal spin-alignment at very low $p_T$, with the $T^{+-} (\lambda_\theta = +1, \lambda_\phi = -1, \lambda_{\phi\theta} = 0)$ scenario resulting in the largest downward variation at $p_T \gtrsim 4 \text{ GeV}$. In this measurement we extend

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure10}
\caption{Differential cross sections multiplied by the di-muon branching fraction, for $\Upsilon$(1S), $\Upsilon$(2S) and $\Upsilon$(3S) production extrapolated to the full phase space, $p_T$-integrated as a function of absolute $T$ rapidity. Points with error bars indicate the results of the measurements with total statistical and systematic errors. Results are shown assuming an isotropic spin-alignment scenario.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{figure11}
\caption{Corrected cross-section measurements in the isotropic spin-alignment scenario. Uncertainties quoted represent statistical, systematic, and luminosity terms, respectively.}
\end{figure}
Fig. 12: Differential cross sections multiplied by the di-muon branching fraction, $d^2\sigma/dp_T dy \times Br(\Upsilon \rightarrow \mu^+\mu^-)$, for $\Upsilon(1S)$ production extrapolated to the full phase space for (top) central and (bottom) forward rapidities. Points with error bars indicate results of the measurements with total (statistical and systematic) uncertainties. The maximal envelope of variation of the result due to spin-alignment uncertainty is indicated by the solid band. Also shown are predictions of direct production with the NNLO* Color Singlet Mechanism (CSM) and inclusive predictions from the Color Evaporation Model (CEM). These theory predictions are shown as a ratio to the data in the lower panes for CEM (middle) and CSM (bottom), along with detail of the variations of the cross-section measurement under the four anisotropic spin-alignment scenarios as a ratio to the nominal data.

In Figs. 12–14 a comparison is also made to two theoretical predictions of $\Upsilon$ production. The first [16], is the $p_T$ range above 45 GeV where the maximal possible impact due to the unknown spin-alignment of $\Upsilon$ is below $\pm 10\%$. This is significantly smaller than the theoretical uncertainties and is of similar magnitude to current experimental uncertainties. As such, this region will offer a precision environment to compare future theoretical studies of $\Upsilon$ production to data.

In Figs. 12–14 a comparison is also made to two theoretical predictions of $\Upsilon$ production. The first [16], is
A QCD-based calculation using the color-singlet mechanism [14], referred to as NNLO* CSM and presumes that \( \Upsilon \) meson production occurs via a color-singlet state and includes full corrections up to next-to-leading order (NLO), as well as some of the most important next-to-next-to-leading-order (NNLO) terms. This inclusion significantly modifies the prediction. The partial nature of the higher-order calculation limits the applicability of the calculation to values above a particular \( \Upsilon \ p_T \) threshold and increases the sensitivity of the prediction to the choice of renormalization and factorization scales.

The second prediction, known as the Color Evaporation Model [19, 31], labeled as CEM, is a phenomenological model for inclusive \( \Upsilon \) production based on quark-hadron duality. This model assumes that any heavy \( QQ \) pair produced in the initial hard scattering evolves to a quarkonium state if its mass is below the threshold of open heavy-flavor meson pairs. Predictions of the CEM model involve a single constant that must be determined from corrected cross-section measurements for each quarkonium state and use a \( b \)-quark mass of 4.75 GeV. As in the case of the CSM, divergences in the predictions restrict the applicability of the model at low \( \Upsilon \ p_T \). Uncertainties from factorization and renormalization scales are estimated from varying the scales independently up and down by a factor of two and additional uncertainties are estimated from varying the \( b \)-quark mass [32].

Color-singlet calculations at NLO/NNLO* predict a largely longitudinal polarization of direct \( \Upsilon \) particularly at high \( p_T \) (although the effect of feed-down introduces large uncertainties to this prediction). The Color Evaporation Model offers no explicit prediction of the spin-alignment evolution of \( \Upsilon \) but the nature of the model suggests no strong polarization should be observed as no single production mechanism dominates.

As can be seen in Figs. 12–14, the two models provide quite different descriptions of \( \Upsilon \) production. Predictions from CSM are for direct \( \Upsilon \) production only, and so do not account for \( \Upsilon \) production that arises from feed-down from the production of higher \( \Upsilon \) states or from radiative decays of the \( \chi_{bJ}(n\pi) \). From previous measurements [33] the contribution of feed-down to \( \Upsilon(1S) \) production is known to be approximately 50%, but the \( p_T \) dependence of the feed-down is not well-known and cannot be reliably predicted and so no explicit correction is made to the CSM predictions shown. No correction is needed for the CEM as this is already an inclusive calculation. Feed-down contributions are expected to similarly contribute to \( \Upsilon(2S) \) production, but no measurement or reliable prediction for the relative contribution exists, so we do not apply a correction to the direct \( \Upsilon(2S) \) CSM predictions either. For \( \Upsilon(3S) \) there is no feed-down from higher \( \Upsilon \) states. Recently, the ATLAS experiment discovered [34] the existence of a state or states interpreted as the \( \chi_{bJ}(3P) \) below the \( BB \) threshold that are expected to have a significant branching fraction for radiative decays into \( \Upsilon(3S) + \gamma \) and thus induce a feed-down contribution to \( \Upsilon(3S) \) (and other \( \Upsilon \) states). As the relative production and decay rates of these states are also as yet unknown no correction is applied to the CSM predictions for \( \Upsilon(3S) \) production either.

For each of the three \( \Upsilon(nS) \) states, the NNLO* CSM predictions (considering also the additional normalization uncertainty due to the poorly-known contributions from feed-down) fit our data well in the moderate \( p_T \) region, but exhibit a steeper \( p_T \) dependence than seen in data. The predictions therefore significantly under-
estimate the cross section at high $p_T$. Theoretical developments in the prediction of feed-down contributions may improve this description. CEM predictions appear to show a better match with data at high $p_T$. These predictions underestimate the rate (favouring a smaller choice of renormalization/factorization scale or larger $b$-quark mass) and have problems in modeling the shape of the spectrum, particularly at lower $p_T$. Shape discrepancies cannot be accommodated within the uncertainties quoted as changes in the scale choice introduce correlated changes in the prediction as a function of $p_T$.

![Image](image1.png)

**FIG. 15:** Differential cross sections multiplied by the di-muon branching fraction, $d\sigma/dy \times Br(\Upsilon \rightarrow \mu^+\mu^-)$, for $\Upsilon(1S)$ production extrapolated to the full phase space. Points with error bars indicate results of the measurements with total (statistical and systematic) uncertainties. The maximal envelope of variation of the result due to spin-alignment uncertainty is indicated by the solid band. The variations of the cross-section measurement under the four anisotropic spin-alignment scenarios are shown in the lower pane as ratios to the unpolarized scenario.

Figures 15 to 17 show the variation of the production cross section as a function of absolute $\Upsilon$ rapidity integrated across all $p_T$. The dependence on rapidity is relatively flat in the interval of rapidities in the ATLAS acceptance.

Variations between spin-alignment scenarios lead largely to a change in the normalization of the distributions with little variation in shape except at high rapidity. There, the $T^{++}$ scenario leads to an increase in the cross section with increasing rapidity, while the fully longitudinal scenario leads to a drop in cross section at high $(|y| \gtrsim 1.7)$ rapidity.

![Image](image2.png)

**FIG. 16:** As for Fig. 15 but for $\Upsilon(2S)$ production.

![Image](image3.png)

**FIG. 17:** As for Fig. 15 but for $\Upsilon(3S)$ production.

**C. Cross section ratios**

From our differential cross-section measurements, we explore the $p_T$ and rapidity dependence of $\Upsilon(2S)$ and $\Upsilon(3S)$ production relative to the $\Upsilon(1S)$ by deriving the ratios

$$\frac{d^2\sigma(pp \rightarrow \Upsilon(nS))/dp_Tdy}{d^2\sigma(pp \rightarrow \Upsilon(1S))/dp_Tdy} \times \frac{Br(\Upsilon(nS) \rightarrow \mu^+\mu^-)}{Br(\Upsilon(1S) \rightarrow \mu^+\mu^-)} \quad (9)$$
for $|y|^\gamma < 2.25$ with $n=2,3$. Such observables are sensitive to the magnitude and kinematic dependencies of feed-down contributions between the three $\Upsilon$ states. Results of the differential cross-section ratio measurements are presented in Figs. 18 and 19.

These measurements are made under the assumption of unpolarized $\Upsilon(nS)$ mesons, and take into account statistical correlations between the fitted numbers of $\Upsilon(1S)$, $\Upsilon(2S)$ and $\Upsilon(3S)$ mesons. Systematic uncertainties are estimated by varying acceptance, efficiency, and fit model assumptions coherently in the numerator and denominator when calculating the ratios, thereby partially canceling uncertainties in the ratio. Luminosity uncertainties cancel entirely.

The measured $\Upsilon(nS)/\Upsilon(1S)$ ratios are relatively constant in the $0 < p_T < 5$ GeV interval at $\sim 20\%$ and $\sim 7\%$ respectively for the $\Upsilon(2S)$ and $\Upsilon(3S)$. At higher $p_T$ a significant and steady rise in the relative production rates of higher $\Upsilon$ states is apparent, in agreement with measurements by CMS [6]. However, at the larger $p_T$ values (above $p_T$ of 30–40 GeV) accessible for the first time with these measurements, evidence of a saturation in this rise is apparent, suggesting that we are probing a regime where direct production dominates over contributions from the decays of excited states. In contrast, the rapidity dependence of these production ratios is quite flat across the full $|y| < 2.25$ rapidity interval.

Higher-order color-singlet calculations are not currently able to predict the evolution of these production ratios in $p_T$ due to the significant feed-down contributions. At leading order in the quark velocity in the perturbative expansion, the production ratio of the direct contributions is proportional to the ratio of the squares of the magnitudes of the wavefunction at the origin (or the partial decay widths), multiplied by the branching fractions to di-muons for each of the states in question. The predicted ratios then are 36% for $\Upsilon(2S)/\Upsilon(1S)$ and
29% for $\Upsilon(3S)/\Upsilon(1S)$ for direct production. At high $p_T$, where the measured production ratio plateaus, the values are somewhat higher than these predictions suggesting that there is some enhancement (with respect to the simple picture above) of the $\Upsilon(2S)$ and $\Upsilon(3S)$ production relative to $\Upsilon(1S)$ production.

VII. CONCLUSIONS

We have measured differential production cross sections and relative production rates for $\Upsilon(1S)$, $\Upsilon(2S)$, and $\Upsilon(3S)$ mesons in $pp$ collisions at $\sqrt{s} = 7$ TeV at the LHC up to $p_T^\Upsilon < 70$ GeV in the rapidity interval $|y^\Upsilon| < 2.25$. The possible impact of the $\Upsilon$ spin-alignment on these measured spectra is also quantified. These measurements are compatible with measurements by the CMS and LHCb collaborations. We have measured integrated corrected cross sections multiplied by the $\Upsilon \rightarrow \mu^+\mu^-$ branching fractions, within the rapidity region $|y^\Upsilon| < 2.25$ of 8.01 ± 0.02 ± 0.36 ± 0.31 nb, 2.05 ± 0.01 ± 0.12 ± 0.08 nb, and 0.92 ± 0.01 ± 0.07 ± 0.04 nb for the $\Upsilon(1S)$, $\Upsilon(2S)$, and $\Upsilon(3S)$, respectively. Uncertainties correspond to statistical, systematic, and luminosity measurement effects.

These cross-section estimates assume unpolarized production corresponding to $\lambda_\Upsilon = \lambda_\phi = \lambda_{\phi\phi} = 0$ in Eq. (3). If the production polarization is fully transverse or longitudinal with no dependence on the azimuthal decay angle $\phi^\Upsilon$, corresponding to $\lambda_\Upsilon = \pm 1$, $\lambda_\phi = \lambda_{\phi\phi} = 0$, the integrated cross sections may vary by up to $(+19, -23)\%$, $(+18, -21)\%$ and $(+17, -19)\%$ respectively for the $\Upsilon(1S)$, $\Upsilon(2S)$ and $\Upsilon(3S)$. However, acceptances correspond to certain non-zero values of $\lambda_\phi$ can become extremely low, especially at low transverse momenta of the muon pair. This would lead to a significant increase of the corrected cross sections in these configurations, up to $+217\%$, $+155\%$ and $+126\%$ for the three $\Upsilon$ states.

We compare our differential cross-section results to predictions from two theoretical approaches describing $\Upsilon$ production. Our measurements find both the NNLO* CSM and the CEM predictions have some problems in describing the normalization and shape of the differential spectra. In particular, NNLO* dramatically underestimates the rate at high transverse momenta, where the data tend to agree better with the CEM. The inclusion of $P$-wave feed-down contributions in these theoretical calculation may help to improve the description. Large scale uncertainties in these predictions allow possible contributions from color-octet terms to contribute to the production rate in addition to singlet diagrams. The differential production ratios indicate that the increase in the production of higher $\Upsilon$ states as a function of $p_T^\Upsilon$ relative to the $\Upsilon(1S)$ observed previously begins to saturate at 30–40 GeV. Above $\sim 40$ GeV, the envelope of possible variations in the differential cross sections due to spin-alignment is reduced to below $\pm 10\%$. This, along with the expected reduction in feed-down contributions, results in a relatively well-controlled region in which to study quarkonium production without the dominant experimental and theoretical effects that complicate such studies at lower $p_T$.

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