The decay $J/\psi \rightarrow \omega \eta$ has been studied, using $225.3 \times 10^6 J/\psi$ events accumulated at BESIII. No significant enhancement near the $\omega \eta$ invariant-mass threshold (denoted as $X(\omega \eta)$) is observed. The upper confidence level of the branching fraction $B(J/\psi \rightarrow \omega X(\omega \eta) \rightarrow \omega \eta)$ is determined to be $3.9 \times 10^{-6}$ at the 95% confidence level. The branching fraction of $J/\psi \rightarrow \omega \eta$ is measured to be $B(J/\psi \rightarrow \omega \eta) = (9.0 \pm 0.2 \text{ (stat.)} \pm 0.9 \text{ (syst.)}) \times 10^{-4}$.

PACS numbers: 13.25.Gv, 12.39.Mk, 13.75.Cs

I. INTRODUCTION

An anomalous enhancement near the threshold of the $p\bar{p}$ system, namely $X(p\bar{p})$, was first observed by the BE- SII experiment in the radiative decay $J/\psi \rightarrow \gamma p\bar{p}$ [3], and it was recently confirmed by the CLEO and BESIII experiments [2,4]. In the BESIII experiment, its mass is measured to be $1859^{+3}_{-10} \text{ (stat.)}^{+5}_{-25} \text{ (syst.)} \text{ MeV}/c^2$ and the total width is $\Gamma < 30 \text{ MeV}/c^2$ at the 90% confidence level (C.L.). While in the BESII experiment, a partial wave analysis (PWA) with a correction for the final-state interaction (FSI) is performed, and the spin-parity of $X(p\bar{p})$ is determined to be $0^{-+}$, its mass is $1832^{+19}_{-17} \text{ (stat.)}^{+18}_{-25} \text{ (syst.)} \text{ MeV}/c^2$ and the total width is $\Gamma < 76 \text{ MeV}/c^2$ at the 90% C.L. [5].

The discovery of $X(p\bar{p})$ stimulated a number of theoretical interpretations and experimental studies [6,11]. There is no experimental evidence of such an enhancement in other quarkonium decays, e.g. $J/\psi \rightarrow \pi^0 p\bar{p}$ [1] or $\Upsilon(2S) \rightarrow \gamma p\bar{p}$ [8]. In $\psi(2S) \rightarrow \gamma p\bar{p}$, the recent BESIII measurement shows a relative production rate to that of $J/\psi$ decays of $R = 5.08\%$ [8]. A number of theoretical speculations have been proposed to interpret the nature of this structure, including baryonium [6,11], a multiquark state [12] or mainly a pure FSI [13,14]. It was proposed to associate this enhancement with a broad enhancement observed in $B$ meson decays [17,18] or a new resonance $X(1835)$ in $J/\psi \rightarrow \gamma \pi^0 \pi^- \eta$ decay at BE- SII [19].

The investigation of the near-threshold $p\bar{p}$ invariant mass spectrum in other $J/\psi$ decay modes will be helpful in understanding the nature of the observed structure. The decay $J/\psi \rightarrow \omega p\bar{p}$ restricts the isospin of the $p\bar{p}$ system, and it is helpful to clarify the role of the $p\bar{p}$ FSI. The BESIII collaboration studied $J/\psi \rightarrow \omega p\bar{p}$ via $\omega$ decaying to $\pi^0 \pi^+ \pi^-$ with a data sample of $5.8 \times 10^7 J/\psi$...
events. No significant signal near the threshold of the $par{p}$ invariant-mass spectrum was observed and an upper limit on the branching fraction of $J/\psi \to \omega X(p\bar{p}) \to \omega p\bar{p}$ was determined to be $1.5 \times 10^{-5}$ at the 90% C.L., which disfavored the interpretation of a pure FSI effect giving rise to the $X(p\bar{p})$. In this paper, the analysis of $J/\psi \to \omega p\bar{p}$ via the decay channel $\omega \to \gamma\pi^0$ is presented, based on a data sample of $(225.3 \pm 2.8) \times 10^6 J/\psi$ events accumulated with the BESIII detector. Searching for the $X(p\bar{p})$ in the decay mode $J/\psi \to \omega p\bar{p} \to \gamma\pi^0 p\bar{p}$ has a particular advantage: a low irreducible background from $N^*$ is expected. The channel $J/\psi \to \omega p\bar{p} \to \pi^0\pi^0 p\bar{p}$ has irreducible background from various $N^*$ decays and $\Delta$ decays, where interferences may have a large impact on the uncertainty of the measurements.

BESIII/BEPCII [21] is a major upgrade of the BESII experiment at the BEPC accelerator [22] for studies of hadron spectroscopy and $\tau$-charm physics [23]. The design peak luminosity of the double-ring $e^+e^-$ collider, BEPCII, is $10^{33} \text{cm}^{-2}\text{s}^{-1}$ at beam currents of 0.93 A. The BESIII detector with a geometrical acceptance of 93% of 4$\pi$, consists of the following main components: 1) a small-celled, helium-based main drift chamber (MDC) with 43 layers. The average single wire resolution is 135 $\mu$m, and the momentum resolution for 1 GeV/$c$ charged particles in a 1 T magnetic field is 0.5%; 2) an electromagnetic calorimeter (EMC) made of 6240 CsI (TI) crystals arranged in a cylindrical shape (barrel) plus two end-caps. For 1.0 GeV photons, the energy resolution is 2.5% in the barrel and 5% in the end-caps, and the position resolution is 6 mm in the barrel and 9 mm in the end-caps; 3) a Time-Of-Flight system (TOF) for particle identification (PID) composed of a barrel part made of two layers with 88 pieces of 5 cm thick, 2.4 m long plastic scintillators in each layer, and two end-caps with 48 fan-shaped, 5 cm thick, plastic scintillators in each end-cap. The time resolution is 80 ps in the barrel, and 110 ps in the end-caps, corresponding to a $\pi/\kappa$ separation by more than 2$\sigma$ for momenta below about 1 GeV/$c^2$; 4) a muon chamber system (MUC) made of 1000 m$^2$ of Resistive Plate Chambers (RPC) arranged in 9 layers in the barrel and 8 layers in the end-caps and incorporated in the return iron yoke of the superconducting magnet. The position resolution is about 2 cm.

The optimization of the event selection and the estimate of physics backgrounds are performed through Monte Carlo (MC) simulations. The GEANT4-based simulation software BOOST [24] includes the geometric and material description of the BESIII detectors and the detector response and digitization models, as well as the tracking of the detector running conditions and performance. The production of the $J/\psi$ resonance is simulated by the MC event generator KKMC [25], while the decays are generated by EVTGEN [26] for known decay modes with branching ratios being set to PDG [27] world average values, and by LUNDCHARM [28] for the remaining unknown decays. The analysis is performed in the framework of the BESIII offline software system [29] which takes care of the detector calibration, event reconstruction and data storage.

II. EVENT SELECTION

Signal $J/\psi \to \omega p\bar{p}$ events with $\omega \to \gamma\pi^0$ final states have the topology $\gamma \gamma \gamma p\bar{p}$. The event candidates are required to have two well reconstructed charged tracks with net charge zero, and at least three photons.

Charged-particle tracks in the polar angle range $|\cos \theta| < 0.93$ are reconstructed from the MDC hits, only tracks in barrel region ($|\cos \theta| < 0.8$) are used to reduce systematic uncertainties in tracking and particle identification. Tracks with their points of closest approach to the beamline within $\pm 10$ cm of the interaction point in the beam direction, and within 1 cm in the plane perpendicular to the beam are selected. TOF and $dE/dx$ information are combined to determine particle identification confidence levels for $\pi$, $K$ and $p(\bar{p})$ hypotheses; and the particle type with highest confidence level is assigned to each track. A proton and an anti-proton are required. To reduce the systematic error due to differences of the tracking efficiency at low momentum between data and MC, the momentum of the proton or anti-proton is further required to be larger than 300 MeV/$c$.

Photon candidates are reconstructed by clustering signals in EMC crystals. The photon candidates are required to be in the barrel region ($|\cos \theta| < 0.8$) of the EMC with at least 25 MeV energy deposition, or in the end-caps region ($0.86 < |\cos \theta| < 0.92$) with at least 50 MeV energy deposition, where $\theta$ is the polar angle of the shower. Timing information from the EMC is used to suppress electronic noise and energy depositions that are unrelated to the event. To suppress showers generated by charged particles, the photon candidates are furthermore required to be separated by an angle larger than 10$^\circ$ and larger than 30$^\circ$ from the proton and anti-proton, respectively.

A four-constraint (4C) energy-momentum conserving kinematic fit is performed to the $\gamma \gamma \gamma p\bar{p}$ hypothesis. For events with more than three photon candidates, the combination with the minimum $\chi^2_{4C}$ is selected, and $\chi^2_{4C} < 30$ is required. The $\pi^0$ candidates are reconstructed from the two of the three selected photons with an invariant mass closest to the $\pi^0$ mass, and $|M_{\gamma\gamma} - M_{\pi^0}| < 15$ MeV/$c^2$ is required.

III. BRANCHING FRACTION AND YIELD MEASUREMENTS

Figure 1 shows the $\gamma\pi^0$ invariant mass spectrum for candidate $J/\psi \to \gamma\pi^0 p\bar{p}$ events, where a distinctive $\omega$ signal is seen. An unbinned maximum likelihood fit is performed to the $\gamma\pi^0$ invariant mass with the $\omega$ signal
Candidate $J/\psi \rightarrow \omega p\bar{p}$ events are selected with the mass window requirement $0.753 \text{ GeV}/c^2 < M(\gamma p^0) < 0.813 \text{ GeV}/c^2$, and the Dalitz plot of these events is shown in Fig. 2. There are no obvious structures in the Dalitz plot, though the distribution is different from the pure $\omega p\bar{p}$ phase space distribution. The corresponding $p\bar{p}$, $\omega p$ and $\omega \bar{p}$ invariant-mass spectra are also presented in Fig. 2. The data points with error bars are from signal region and the hatched area are from the sideband region. The mass threshold is shown in Fig. 3.

To obtain the number of $J/\psi \rightarrow \omega X(p\bar{p}) \rightarrow \omega p\bar{p}$ events, an unbinned maximum likelihood fit is performed to the $p\bar{p}$ invariant mass around the mass threshold. In the fit, the spin-parity of $X(p\bar{p})$ is assumed to be $0^-$, and the signal of $X(p\bar{p})$ in the $J/\psi \rightarrow \omega X(p\bar{p}) \rightarrow \omega p\bar{p}$ decay is parametrized by an acceptance-weighted $S$-wave Breit-Wigner function:

$$BW(M) \simeq \frac{a^{2L+1}k^3}{(M^2 - M_0^2)^2 + M_0^2 k^2} \times \varepsilon_{\text{rec}}(M).$$

(2)

Here, $q$ is the momentum of the proton in the $p\bar{p}$ rest frame; $k$ is the the momentum of the $\omega$ meson; $L = 0$ is the relative orbital angular momentum; $M$ is the invariant mass of $p\bar{p}$; $M_0$ and $\Gamma$ are the mass and width of the $X(p\bar{p})$, respectively, which are taken from BES-I/II results [3]; $\varepsilon_{\text{rec}}$ is the detection efficiency. The non-resonant $J/\psi \rightarrow \omega p\bar{p}$ events are also described by the function $f(\delta) = N(\delta^{1/2} + a_1\delta^{3/2} + a_2\delta^{5/2})$ with $\delta = M_{p\bar{p}} - 2m_p$ where $m_p$ is the proton mass. The normalization and shape parameters $a_1$ and $a_2$ are determined by a simultaneous fit to the $M(p\bar{p})$ in $\omega$ signal region and $\omega$ sideband region $0.09 \text{ GeV}/c^2 < |M(\gamma p^0) - 0.783| < 0.12 \text{ GeV}/c^2$.

The branching fraction of $J/\psi \rightarrow \omega p\bar{p}$ is calculated according to:

$$B(J/\psi \rightarrow \omega p\bar{p}) = \frac{N_{\text{obs}}}{N_{J/\psi} \times B(\omega \rightarrow \gamma p^0) \times B(\pi^0 \rightarrow \gamma \gamma) \times \varepsilon_{\text{rec}}}.$$ (1)

where $N_{\text{obs}}$ is the number of signal events determined from the fit to the $\gamma p^0$ invariant mass; $N_{J/\psi}$ is the number of $J/\psi$ events [20]; $B(\omega \rightarrow \gamma p^0)$ and $B(\pi^0 \rightarrow \gamma \gamma)$ are branching fractions of $\omega \rightarrow \gamma p^0$ and $\pi^0 \rightarrow \gamma \gamma$, respectively, as from the PDG [27]; and the detection efficiency $\varepsilon_{\text{rec}}$ is $(16.1 \pm 1.7\%$ obtained from a MC sample for $J/\psi \rightarrow \omega p\bar{p}$ events generated according to a phase-space distribution. The measured branching fraction is

$$B(J/\psi \rightarrow \omega p\bar{p}) = (9.0 \pm 0.2 \text{ (stat.)}) \times 10^{-4}.$$
where \( \sigma_{\text{sys.}} \) is the total systematic uncertainty which will be described in the next section. The upper limit on the product of branching fractions is 
\[
B(J/\psi \rightarrow \omega X(p\bar{p}) \rightarrow \omega p \bar{p}) < 3.9 \times 10^{-6}
\]
at the 95% C.L..

An alternative fit with a Breit-Wigner function including the Jülich FSI

\[
BW(M) \simeq \frac{f_{\text{FSI}} \times q^{2L+1}k^3}{(M^2 - M_0^2)^2 + M_0^2T^2} \times \varepsilon_{\text{rec}}(M),
\]

for \( X(p\bar{p}) \) is performed. Here, \( f_{\text{FSI}} \) is the Jülich FSI correction factor [14]. The mass and width of \( X(p\bar{p}) \) are taken from the previous BESIII PWA results [2]. The upper limit on the product of branching fractions is determined to be 
\[
B(J/\psi \rightarrow \omega X(p\bar{p}) \rightarrow \omega p \bar{p}) < 3.7 \times 10^{-6}
\]
at the 95% C.L..

### IV. SYSTEMATIC UNCERTAINTIES

Several sources of systematic uncertainties are considered in the measurement of the branching fractions. These include differences between data and the MC simulation for the tracking algorithm, the PID, photon detection, the kinematic fit, as well as the fitting procedure, the branching fraction of the intermediate states and the total number of \( J/\psi \) events.

The systematic uncertainties associated with the tracking efficiency and PID efficiency have been studied with \( J/\psi \rightarrow p\bar{p}\pi^+\pi^- \) using a technique similar to that discussed in Ref. [31]. The difference of tracking efficiencies between data and MC simulation is 2% per charged track. The systematic uncertainty from PID is 2% per proton (anti-proton).

The photon detection systematic uncertainty is studied by comparing the photon efficiency between MC simulation and the control sample \( J/\psi \rightarrow \rho \pi \). The relative efficiency difference is about 1% for each photon [32, 33].
Here, 3% is taken as the systematic error for the efficiency of detecting three photons. The uncertainty due to $\pi^0$ reconstruction efficiency is taken as 1%.

To estimate the uncertainty associated with the kinematic fit, selected samples of $J/\psi \rightarrow \Sigma^+ \Sigma^- \rightarrow p \pi^0 \bar{p} \pi^0$ events are used. The kinematic fit efficiency is defined as the ratio between the signal yield of $\Sigma^+$ with or without the kinematic fit. The difference of kinematic fit efficiency between data and MC is 3%, and is taken as the systematic uncertainty caused by the kinematic fit.

As described above, the yield of $J/\psi \rightarrow \omega p \bar{p}$ is derived from a fit to the invariant-mass spectrum of $\gamma \pi^0$ pairs. To evaluate the systematic uncertainty associated with the fitting procedure, the following two aspects are studied (i) Fitting region: In the nominal fit, the mass spectrum of $\gamma \pi^0$ is fitted in the range from 0.663 GeV/c$^2$ to 0.903 GeV/c$^2$. Alternative fits within ranges 0.653 GeV/c$^2$ to 0.913 GeV/c$^2$ and 0.673 GeV/c$^2$ to 0.893 GeV/c$^2$ are performed, and the difference in the signal yield of 2% is taken as the systematic uncertainty associated with the fit interval. (ii) Background shape: To estimate the uncertainty due to the background parametrization for the branching fraction $B(J/\psi \rightarrow \omega p \bar{p})$, a first or third order instead of a second-order Chebychev polynomial is used in the fitting. The difference of 1.2% is used as an estimate of the systematic uncertainty.

For the upper limit on the branching fraction $B(J/\psi \rightarrow \omega p \bar{p})$, the systematic uncertainty associated with the fitting procedure is estimated by fixing the shape of the non-resonant contribution to a phase space MC simulation of $J/\psi \rightarrow \omega p \bar{p}$, which is presented by Figure. 4; enlarging/reducing the normalization of the non-$\omega$ contribution by 7% (the difference of the estimation of non-$\omega$ background level between data and inclusive MC); and varying the sideband region to 0.095 GeV/c$^2 < |M(\gamma \pi^0) - 0.783| < 0.115$ GeV/c$^2$ and 0.085 GeV/c$^2 < |M(\gamma \pi^0) - 0.783| < 0.125$ GeV/c$^2$.

When fitting with or without the FSI effect, the signal yields for the alternative fits are lower or equal to the nominal fit, therefore the conservative upper limit from the fit without FSI correction is reported.

Various distributions obtained with data and the phase-space MC sample have been compared and some discrepancies are observed. To determine the systematic error on the detection efficiency associated with these discrepancies, an alternative detection efficiency is estimated by the re-weighting phase-space MC samples. The difference in detection efficiency compared to the nominal one is 7% and taken as a systematic uncertainty. The number of $J/\psi$ events is determined from an inclusive analysis of $J/\psi$ hadronic events and an uncertainty of 1.24% is associated to it. The uncertainties due to the branching fractions of $\omega \rightarrow \gamma \pi^0$ and $\pi^0 \rightarrow \gamma \gamma$ are taken from the PDG.
In summary, using $\left(225.3 \pm 2.8 \times 10^6\right) J/\psi$ events collected with the BESIII detector, the decay of $J/\psi \to \omega p\bar{p}$ in the decay mode $\omega \to \gamma \pi^0$ is studied. The branching fraction $B(J/\psi \to \omega p\bar{p})$ is measured to be $(9.0 \pm 0.2 \text{ (stat.)} \pm 0.9 \text{ (syst.)}) \times 10^{-4}$. No obvious enhancement around the $p\bar{p}$ invariant-mass threshold is observed. At the 95% C.L., the upper limits on the product of branching fractions $B(J/\psi \to \omega X(p\bar{p}) \to p\bar{p})$ are measured to be $3.7 \times 10^{-6}$ and $3.9 \times 10^{-6}$ with and without accounting for the Jülich FSI effect, respectively. As isospin for $J/\psi \to \gamma p\bar{p}$ and $\omega p\bar{p}$ should both favor $I = 0$ ($I = 1$ should be suppressed in $J/\psi \to \gamma p\bar{p}$ as in other $J/\psi$ radiative decays), the non-observation of $X(p\bar{p})$ in $p\bar{p}$ disfavors the pure FSI interpretation for the $p\bar{p}$ threshold enhancement in the decay $J/\psi \to \gamma p\bar{p}$.

VI. ACKNOWLEDGMENT

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TABLE I. Summary of systematic uncertainties. '-' means the corresponding systematic uncertainty is negligible.

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<th>Source</th>
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<th>Upper limit of $B(J/\psi \to \omega X(p\bar{p}) \to p\bar{p})$</th>
<th>Upper limit of $B(J/\psi \to \omega X(p\bar{p}) \to p\bar{p})$ with FSI</th>
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